

Graduate Aptitude Test in Engineering 2017

Question Paper Name: Electronics and Communication Engineering 5th Feb 2017 session 2
Subject Name: Electronics and Communication Engineering
Duration: 180
Total Marks: 100



Organizing Institute: Indian Institute of Technology Roorkee



Question Number : 1

Correct : 1 Wrong : 0

The rank of the matrix

$$\begin{bmatrix} 1 & -1 & 0 & 0 & 0 \\ 0 & 0 & 1 & -1 & 0 \\ 0 & 1 & -1 & 0 & 0 \\ -1 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 & -1 \end{bmatrix}$$

is _____.

Question Number : 2

Correct : 1 Wrong : -0.33

The general solution of the differential equation

$$\frac{d^2y}{dx^2} + 2\frac{dy}{dx} - 5y = 0$$

in terms of arbitrary constants K_1 and K_2 is

(A) $K_1 e^{(-1+\sqrt{6})x} + K_2 e^{(-1-\sqrt{6})x}$

(B) $K_1 e^{(-1+\sqrt{8})x} + K_2 e^{(-1-\sqrt{8})x}$

(C) $K_1 e^{(-2+\sqrt{6})x} + K_2 e^{(-2-\sqrt{6})x}$

(D) $K_1 e^{(-2+\sqrt{8})x} + K_2 e^{(-2-\sqrt{8})x}$

Question Number : 3

Correct : 1 Wrong : 0

The smaller angle (in degrees) between the planes $x + y + z = 1$ and $2x - y + 2z = 0$ is _____.

Question Number : 4

Correct : 1 Wrong : -0.33

The residues of a function

$$f(z) = \frac{1}{(z-4)(z+1)^3}$$

are

(A) $\frac{-1}{27}$ and $\frac{-1}{125}$

(B) $\frac{1}{125}$ and $\frac{-1}{125}$

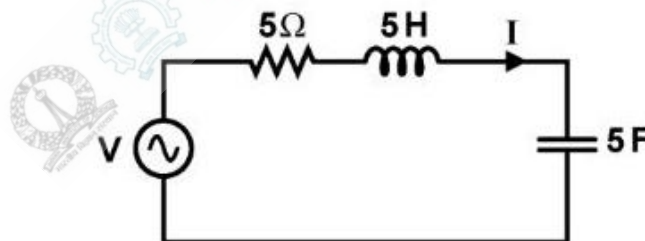
(C) $\frac{-1}{27}$ and $\frac{1}{5}$

(D) $\frac{1}{125}$ and $\frac{-1}{5}$

Question Number : 5

Correct : 1 Wrong : 0

In the circuit shown, V is a sinusoidal voltage source. The current I is in phase with voltage V . The ratio $\frac{\text{amplitude of voltage across the capacitor}}{\text{amplitude of voltage across the resistor}}$ is _____.



Question Number : 6

Correct : 1 Wrong : 0

A connection is made consisting of resistance A in series with a parallel combination of resistances B and C . Three resistors of value $10\ \Omega$, $5\ \Omega$, $2\ \Omega$ are provided. Consider all possible permutations of the given resistors into the positions A , B , C , and identify the configurations with maximum possible overall resistance, and also the ones with minimum possible overall resistance. The ratio of maximum to minimum values of the resistances (up to second decimal place) is _____.

Question Number : 7**Correct : 1 Wrong : -0.33**

An LTI system with unit sample response $h[n] = 5\delta[n] - 7\delta[n - 1] + 7\delta[n - 3] - 5\delta[n - 4]$ is a

- (A) low-pass filter (B) high-pass filter
(C) band-pass filter (D) band-stop filter

Question Number : 8**Correct : 1 Wrong : -0.33**

The input $x(t)$ and the output $y(t)$ of a continuous-time system are related as

$$y(t) = \int_{t-T}^t x(u) du.$$

The system is

- (A) linear and time-variant (B) linear and time-invariant
(C) non-linear and time-variant (D) non-linear and time-invariant

Question Number : 9**Correct : 1 Wrong : -0.33**

An n -channel enhancement mode MOSFET is biased at $V_{GS} > V_{TH}$ and $V_{DS} > (V_{GS} - V_{TH})$, where V_{GS} is the gate-to-source voltage, V_{DS} is the drain-to-source voltage and V_{TH} is the threshold voltage. Considering channel length modulation effect to be significant, the MOSFET behaves as a

- (A) voltage source with zero output impedance
(B) voltage source with non-zero output impedance
(C) current source with finite output impedance
(D) current source with infinite output impedance

Question Number : 10**Correct : 1 Wrong : -0.33**

An *npn* bipolar junction transistor (BJT) is operating in the active region. If the reverse bias across the base-collector junction is increased, then

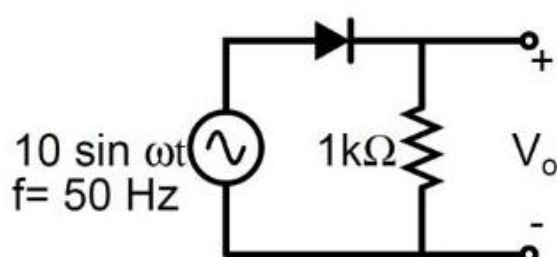
- (A) the effective base width increases and common-emitter current gain increases
- (B) the effective base width increases and common-emitter current gain decreases
- (C) the effective base width decreases and common-emitter current gain increases
- (D) the effective base width decreases and common-emitter current gain decreases

Question Number : 11**Correct : 1 Wrong : 0**

Consider an *n*-channel MOSFET having width W , length L , electron mobility in the channel μ_n and oxide capacitance per unit area C_{ox} . If gate-to-source voltage $V_{GS} = 0.7$ V, drain-to-source voltage $V_{DS} = 0.1$ V, $(\mu_n C_{ox}) = 100 \mu\text{A}/\text{V}^2$, threshold voltage $V_{TH} = 0.3$ V and $(W/L) = 50$, then the transconductance g_m (in mA/V) is _____

Question Number : 12**Correct : 1 Wrong : 0**

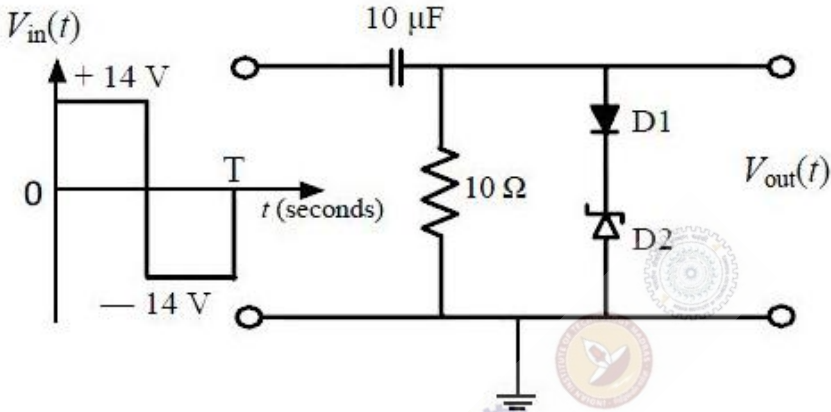
The output V_o of the diode circuit shown in the figure is connected to an averaging DC voltmeter. The reading on the DC voltmeter in Volts, neglecting the voltage drop across the diode, is _____.



Question Number : 13

Correct : 1 Wrong : -0.33

In the figure, D1 is a real silicon *pn* junction diode with a drop of 0.7 V under forward bias condition and D2 is a Zener diode with breakdown voltage of -6.8 V. The input $V_{in}(t)$ is a periodic square wave of period T, whose one period is shown in the figure.



Assuming $10\tau \ll T$, where τ is the time constant of the circuit, the maximum and minimum values of the output waveform are respectively,

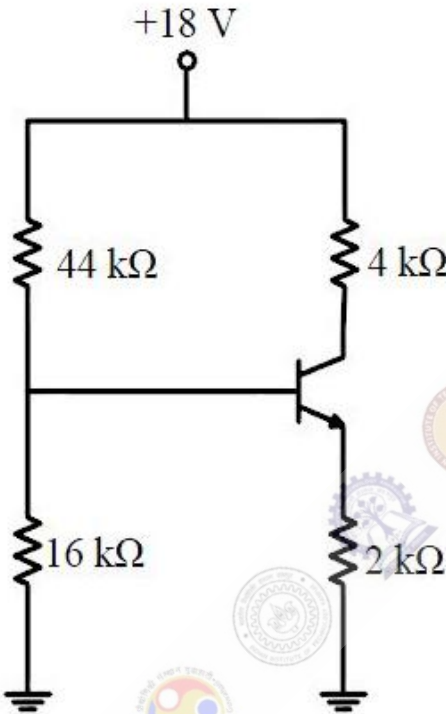
(A) 7.5 V and -20.5 V

(B) 6.1 V and -21.9 V

(C) 7.5 V and -21.2 V

(D) 6.1 V and -22.6 V

Consider the circuit shown in the figure. Assume base-to-emitter voltage $V_{BE} = 0.8 \text{ V}$ and common-base current gain (α) of the transistor is unity.

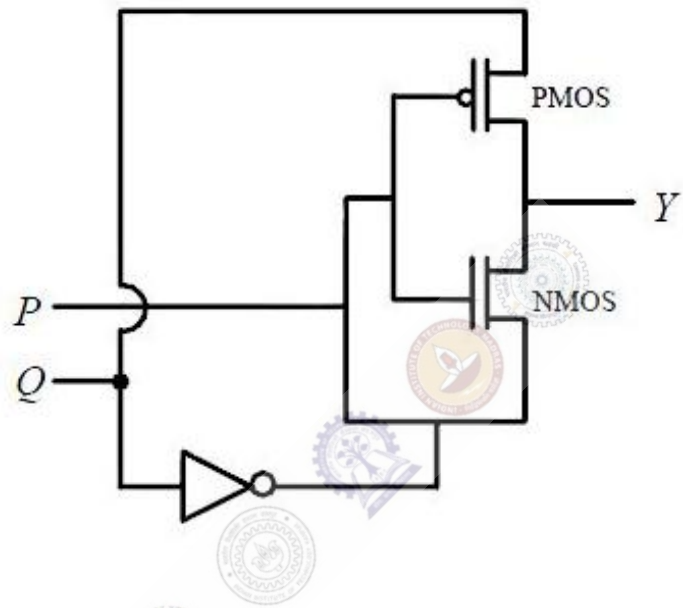


The value of the collector-to-emitter voltage V_{CE} (in volt) is _____

Question Number : 15

Correct : 1 Wrong : -0.33

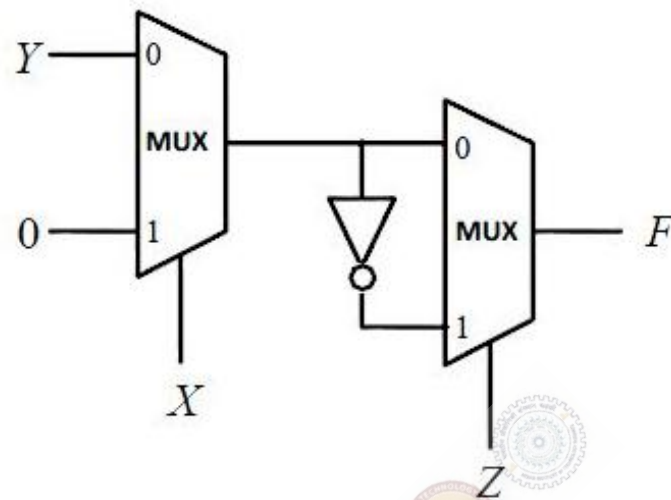
For the circuit shown in the figure, P and Q are the inputs and Y is the output.



The logic implemented by the circuit is

- (A) XNOR
- (B) XOR
- (C) NOR
- (D) OR

Consider the circuit shown in the figure.



The Boolean expression F implemented by the circuit is

(A) $\bar{X}\bar{Y}\bar{Z} + XY + \bar{Y}Z$

(B) $\bar{X}Y\bar{Z} + XZ + \bar{Y}Z$

(C) $\bar{X}Y\bar{Z} + XY + \bar{Y}Z$

(D) $\bar{X}\bar{Y}\bar{Z} + XZ + \bar{Y}Z$

In a DRAM,

(A) periodic refreshing is not required

(B) information is stored in a capacitor

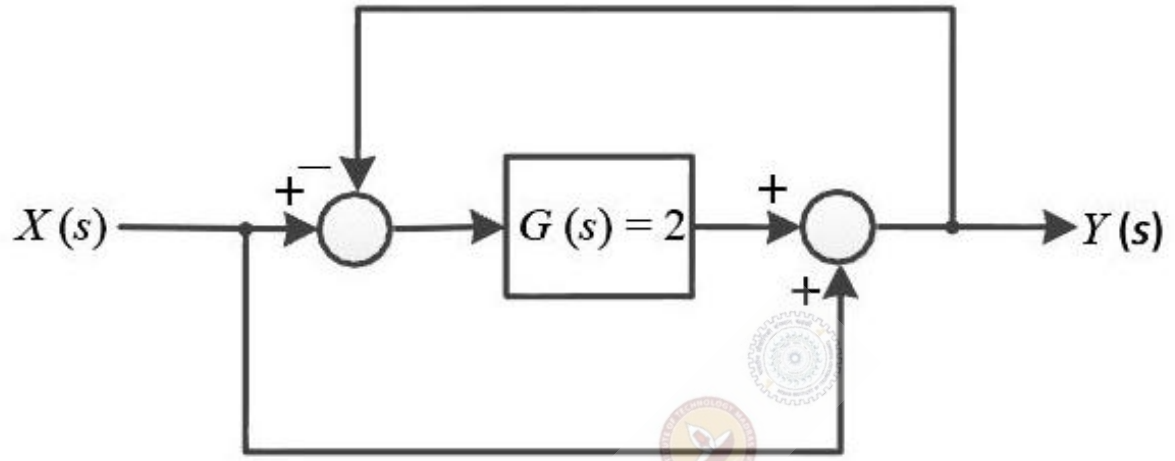
(C) information is stored in a latch

(D) both read and write operations can be performed simultaneously

Question Number : 18

Correct : 1 Wrong : 0

For the system shown in the figure, $Y(s)/X(s) =$ _____



Question Number : 19

Correct : 1 Wrong : 0

Consider the state space realization

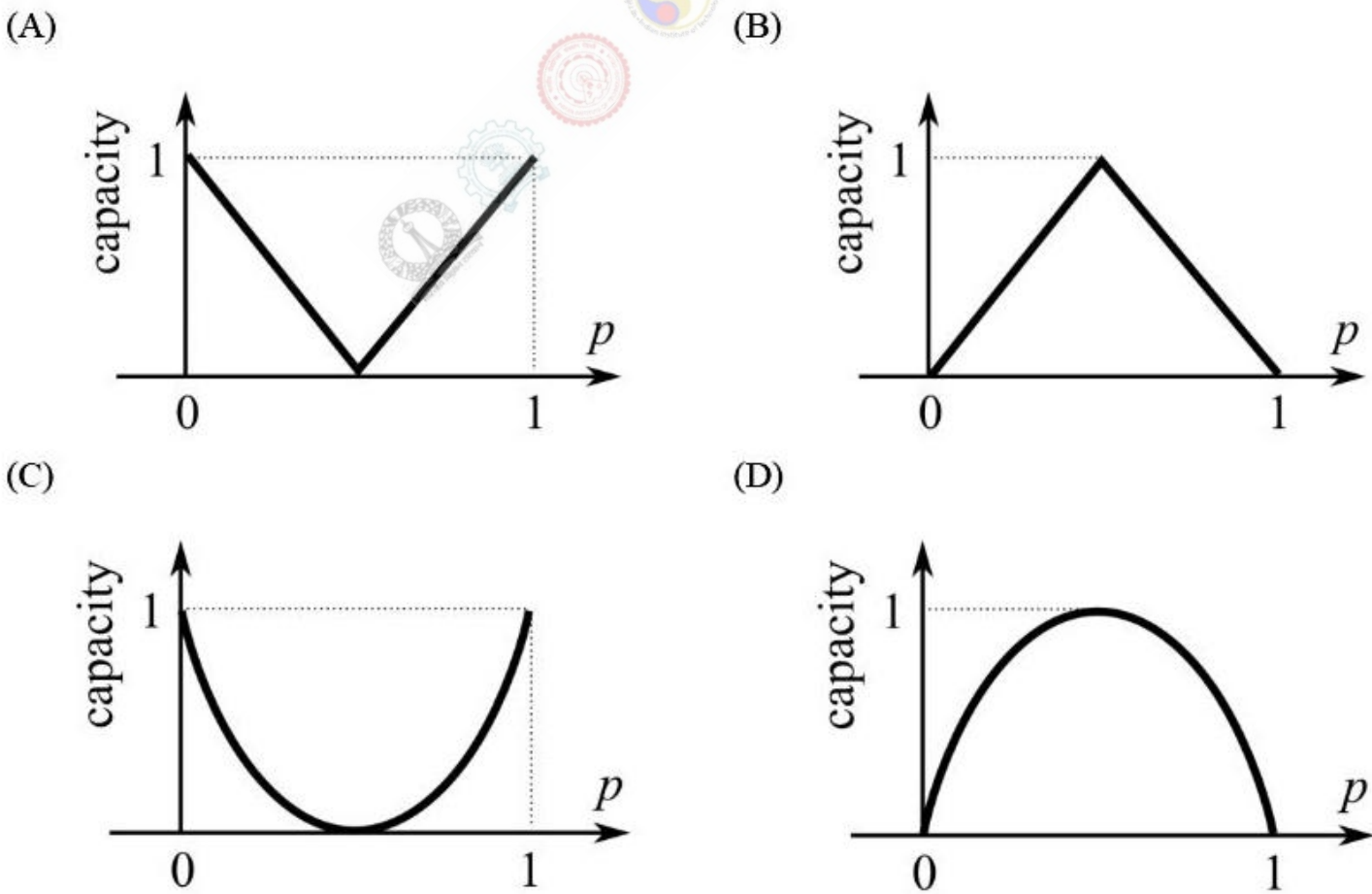
$$\begin{bmatrix} \dot{x}_1(t) \\ \dot{x}_2(t) \end{bmatrix} = \begin{bmatrix} 0 & 0 \\ 0 & -9 \end{bmatrix} \begin{bmatrix} x_1(t) \\ x_2(t) \end{bmatrix} + \begin{bmatrix} 0 \\ 45 \end{bmatrix} u(t), \text{ with the initial condition } \begin{bmatrix} x_1(0) \\ x_2(0) \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix},$$

where $u(t)$ denotes the unit step function. The value of $\lim_{t \rightarrow \infty} \sqrt{x_1^2(t) + x_2^2(t)}$ is _____.

Which of the following statements is **incorrect**?

- (A) Lead compensator is used to reduce the settling time.
- (B) Lag compensator is used to reduce the steady state error.
- (C) Lead compensator may increase the order of a system.
- (D) Lag compensator always stabilizes an unstable system.

Which one of the following graphs shows the Shannon capacity (channel capacity) in bits of a memoryless binary symmetric channel with crossover probability p ?



Question Number : 22

Correct : 1 Wrong : 0

Consider the random process

$$X(t) = U + Vt,$$

where U is a zero-mean Gaussian random variable and V is a random variable uniformly distributed between 0 and 2. Assume that U and V are statistically independent. The mean value of the random process at $t = 2$ is _____

Question Number : 23

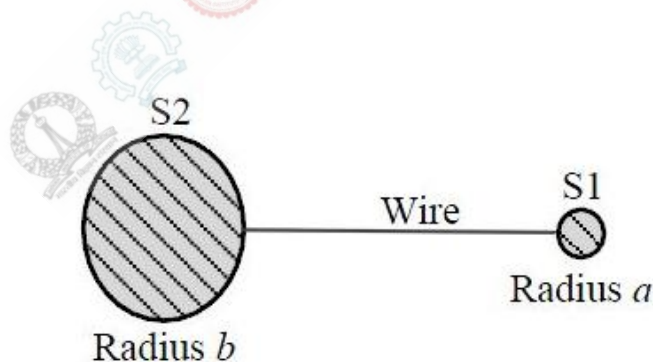
Correct : 1 Wrong : 0

A sinusoidal message signal is converted to a PCM signal using a uniform quantizer. The required signal-to-quantization noise ratio (SQNR) at the output of the quantizer is 40 dB. The minimum number of bits per sample needed to achieve the desired SQNR is _____

Question Number : 24

Correct : 1 Wrong : -0.33

Two conducting spheres S1 and S2 of radii a and b ($b > a$) respectively, are placed far apart and connected by a long, thin conducting wire, as shown in the figure.



For some charge placed on this structure, the potential and surface electric field on S1 are V_a and E_a , and that on S2 are V_b and E_b , respectively. Then, which of the following is **CORRECT**?

(A) $V_a = V_b$ and $E_a < E_b$

(B) $V_a > V_b$ and $E_a > E_b$

(C) $V_a = V_b$ and $E_a > E_b$

(D) $V_a > V_b$ and $E_a = E_b$

Question Number : 25

Correct : 1 Wrong : 0

A two-wire transmission line terminates in a television set. The VSWR measured on the line is 5.8. The percentage of power that is reflected from the television set is _____

Question Number : 26

Correct : 2 Wrong : -0.66

The values of the integrals

$$\int_0^1 \left(\int_0^1 \frac{x-y}{(x+y)^3} dy \right) dx$$

and

$$\int_0^1 \left(\int_0^1 \frac{x-y}{(x+y)^3} dx \right) dy$$

are

- (A) same and equal to 0.5
- (B) same and equal to -0.5
- (C) 0.5 and -0.5 , respectively
- (D) -0.5 and 0.5, respectively

Question Number : 27**Correct : 2 Wrong : -0.66**

An integral I over a counterclockwise circle C is given by

$$I = \oint_C \frac{z^2 - 1}{z^2 + 1} e^z dz.$$

If C is defined as $|z| = 3$, then the value of I is

- (A) $-\pi i \sin(1)$ (B) $-2\pi i \sin(1)$ (C) $-3\pi i \sin(1)$ (D) $-4\pi i \sin(1)$

Question Number : 28**Correct : 2 Wrong : -0.66**

If the vector function $\vec{F} = \hat{a}_x(3y - k_1z) + \hat{a}_y(k_2x - 2z) - \hat{a}_z(k_3y + z)$ is irrotational, then the values of the constants k_1 , k_2 and k_3 , respectively, are

- (A) 0.3, -2.5, 0.5 (B) 0.0, 3.0, 2.0
 (C) 0.3, 0.33, 0.5 (D) 4.0, 3.0, 2.0

Question Number : 29**Correct : 2 Wrong : 0**

Passengers try repeatedly to get a seat reservation in any train running between two stations until they are successful. If there is 40% chance of getting reservation in any attempt by a passenger, then the average number of attempts that passengers need to make to get a seat reserved is _____.

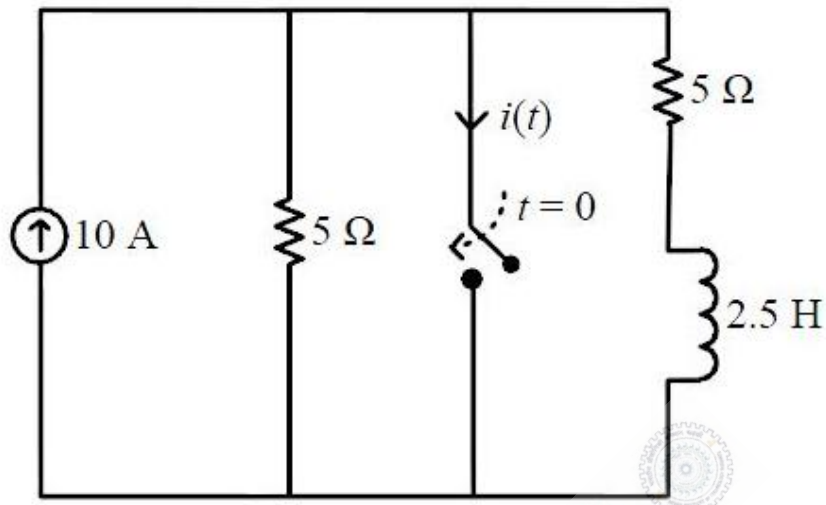
Question Number : 30**Correct : 2 Wrong : 0**

The minimum value of the function $f(x) = \frac{1}{3}x(x^2 - 3)$ in the interval $-100 \leq x \leq 100$ occurs at $x = \underline{\hspace{2cm}}$.

Question Number : 31

Correct : 2 Wrong : 0

The switch in the circuit, shown in the figure, was open for a long time and is closed at $t = 0$.

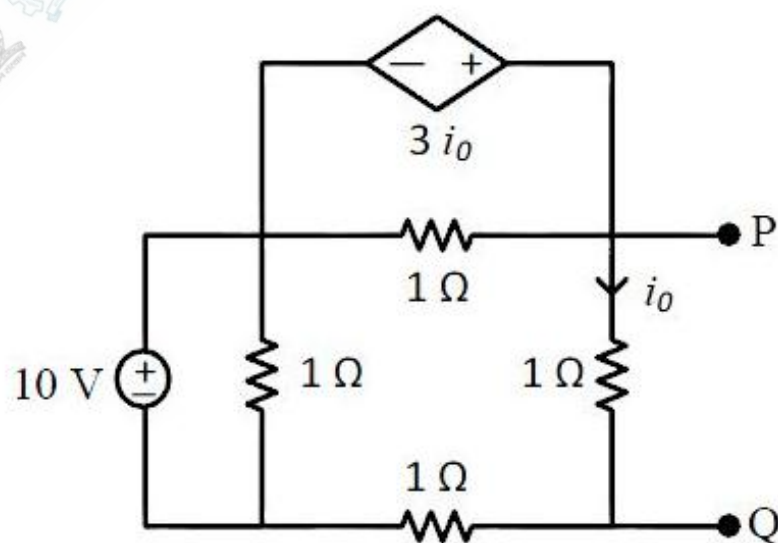


The current $i(t)$ (in ampere) at $t = 0.5$ seconds is _____

Question Number : 32

Correct : 2 Wrong : 0

Consider the circuit shown in the figure.



The Thevenin equivalent resistance (in Ω) across P-Q is _____

Question Number : 33

Correct : 2 Wrong : 0

Consider an LTI system with magnitude response

$$|H(f)| = \begin{cases} 1 - \frac{|f|}{20}, & |f| \leq 20 \\ 0, & |f| > 20 \end{cases}$$

and phase response

$$\arg \{H(f)\} = -2f.$$

If the input to the system is

$$x(t) = 8 \cos\left(20\pi t + \frac{\pi}{4}\right) + 16 \sin\left(40\pi t + \frac{\pi}{8}\right) + 24 \cos\left(80\pi t + \frac{\pi}{16}\right).$$

then the average power of the output signal $y(t)$ is _____

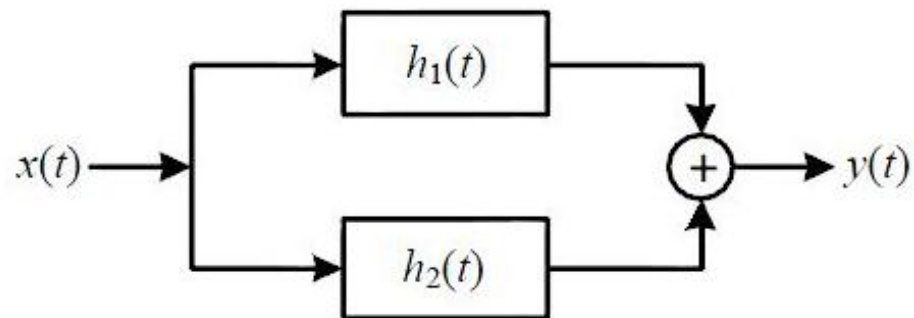
Question Number : 34

Correct : 2 Wrong : 0

The transfer function of a causal LTI system is $H(s) = 1/s$. If the input to the system is $x(t) = [\sin(t)/\pi t] u(t)$, where $u(t)$ is a unit step function, the system output $y(t)$ as $t \rightarrow \infty$ is _____

Question Number : 35**Correct : 2 Wrong : 0**

Consider the parallel combination of two LTI systems shown in the figure.



The impulse responses of the systems are

$$h_1(t) = 2\delta(t + 2) - 3\delta(t + 1)$$

$$h_2(t) = \delta(t - 2).$$

If the input $x(t)$ is a unit step signal, then the energy of $y(t)$ is _____

Question Number : 36**Correct : 2 Wrong : 0**

A MOS capacitor is fabricated on p -type Si (Silicon) where the metal work function is 4.1 eV and electron affinity of Si is 4.0 eV. $E_C - E_F = 0.9$ eV, where E_C and E_F are the conduction band minimum and the Fermi energy levels of Si, respectively. Oxide $\epsilon_r = 3.9$, $\epsilon_o = 8.85 \times 10^{-14}$ F/cm, oxide thickness $t_{ox} = 0.1 \mu\text{m}$ and electronic charge $q = 1.6 \times 10^{-19}$ C. If the measured flat band voltage of this capacitor is -1 V, then the magnitude of the fixed charge at the oxide-semiconductor interface, in nC/cm², is _____.

Question Number : 37**Correct : 2 Wrong : 0**

For a particular intensity of incident light on a silicon pn junction solar cell, the photocurrent density (J_L) is 2.5 mA/cm² and the open-circuit voltage (V_{oc}) is 0.451 V. Consider thermal voltage (V_T) to be 25 mV. If the intensity of the incident light is increased by 20 times, assuming that the temperature remains unchanged, V_{oc} (in volts) will be _____

Question Number : 38**Correct : 2 Wrong : -0.66**

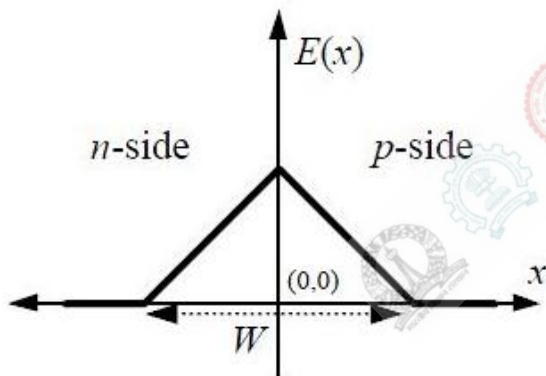
Two n -channel MOSFETs, T1 and T2, are identical in all respects except that the width of T2 is double that of T1. Both the transistors are biased in the saturation region of operation, but the gate overdrive voltage ($V_{GS} - V_{TH}$) of T2 is double that of T1, where V_{GS} and V_{TH} are the gate-to-source voltage and threshold voltage of the transistors, respectively. If the drain current and transconductance of T1 are I_{D1} and g_{m1} respectively, the corresponding values of these two parameters for T2 are

- (A) $8I_{D1}$ and $2g_{m1}$ (B) $8I_{D1}$ and $4g_{m1}$ (C) $4I_{D1}$ and $4g_{m1}$ (D) $4I_{D1}$ and $2g_{m1}$

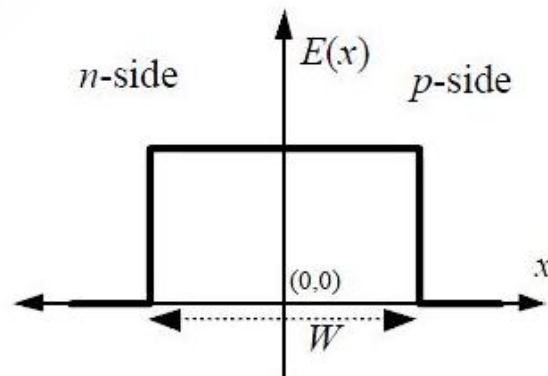
Question Number : 39**Correct : 2 Wrong : -0.66**

An abrupt pn junction (located at $x = 0$) is uniformly doped on both p and n sides. The width of the depletion region is W and the electric field variation in the x -direction is $E(x)$. Which of the following figures represents the electric field profile near the pn junction?

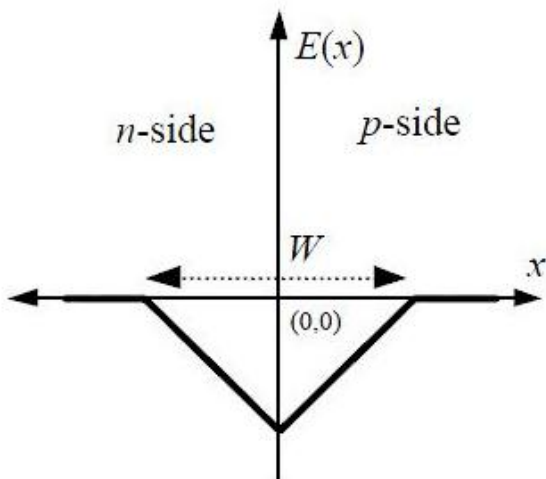
(A)



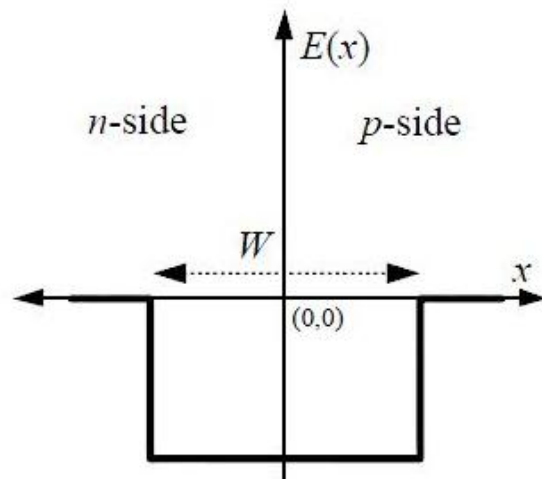
(B)



(C)

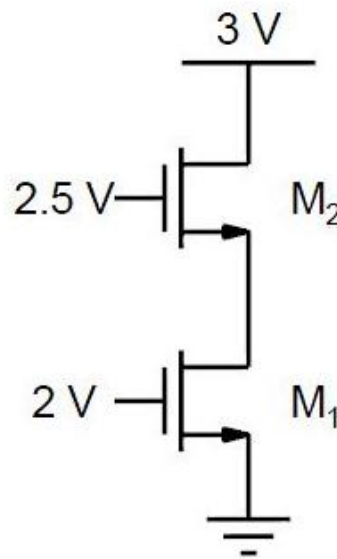


(D)



Question Number : 40**Correct : 2 Wrong : -0.66**

Assuming that transistors M_1 and M_2 are identical and have a threshold voltage of 1 V, the state of transistors M_1 and M_2 are respectively



(A) Saturation, Saturation

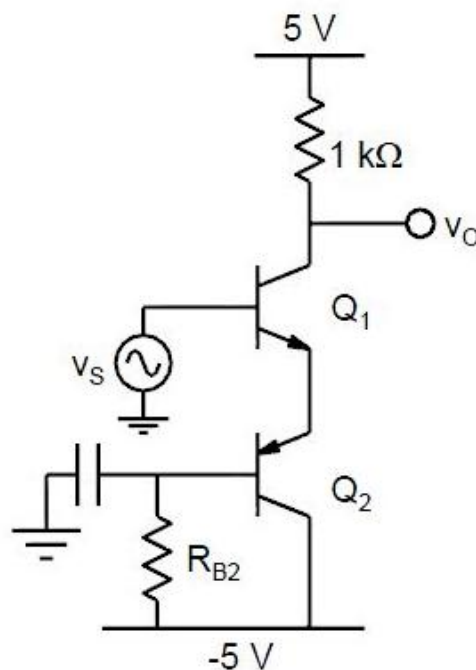
(B) Linear, Linear

(C) Linear, Saturation

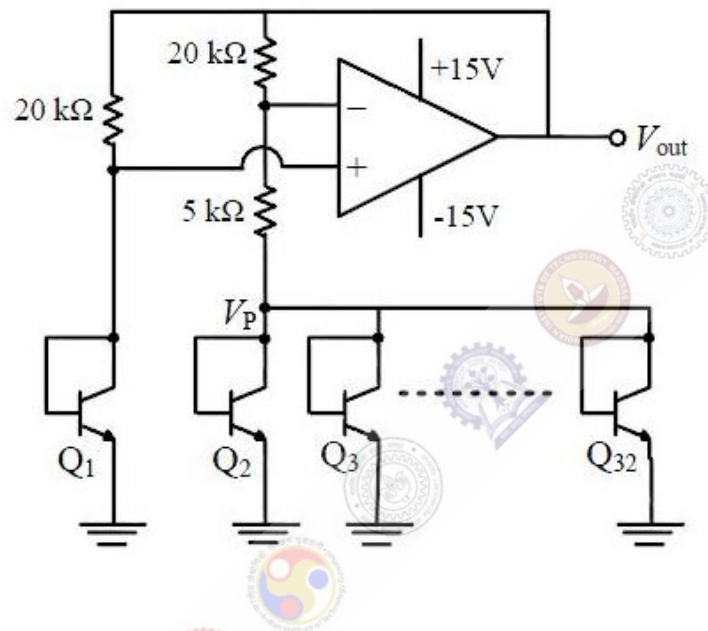
(D) Saturation, Linear

Question Number : 41**Correct : 2 Wrong : 0**

In the circuit shown, transistors Q_1 and Q_2 are biased at a collector current of 2.6 mA. Assuming that transistor current gains are sufficiently large to assume collector current equal to emitter current and thermal voltage of 26 mV, the magnitude of voltage gain V_o/V_s in the mid-band frequency range is _____ (up to second decimal place).

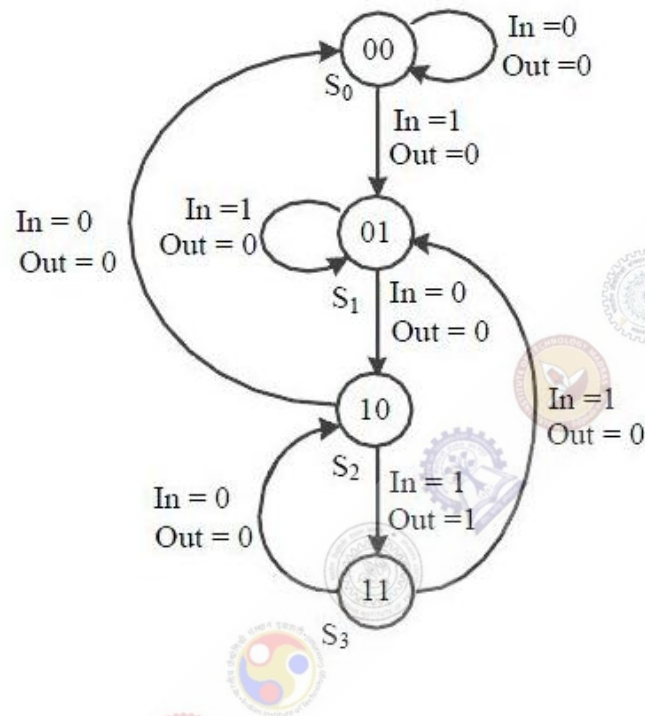


In the voltage reference circuit shown in the figure, the op-amp is ideal and the transistors Q_1, Q_2, \dots, Q_{32} are identical in all respects and have infinitely large values of common-emitter current gain (β). The collector current (I_C) of the transistors is related to their base-emitter voltage (V_{BE}) by the relation $I_C = I_S \exp(V_{BE}/V_T)$, where I_S is the saturation current. Assume that the voltage V_P shown in the figure is 0.7 V and the thermal voltage $V_T = 26$ mV.



The output voltage V_{out} (in volts) is _____

The state diagram of a finite state machine (FSM) designed to detect an overlapping sequence of three bits is shown in the figure. The FSM has an input 'In' and an output 'Out'. The initial state of the FSM is S_0 .



If the input sequence is 10101101001101, starting with the left-most bit, then the number of times 'Out' will be 1 is _____

Question Number : 44

Correct : 2 Wrong : 0

Figure I shows a 4-bit ripple carry adder realized using full adders and Figure II shows the circuit of a full-adder (FA). The propagation delay of the XOR, AND and OR gates in Figure II are 20 ns, 15 ns and 10 ns, respectively. Assume all the inputs to the 4-bit adder are initially reset to 0.

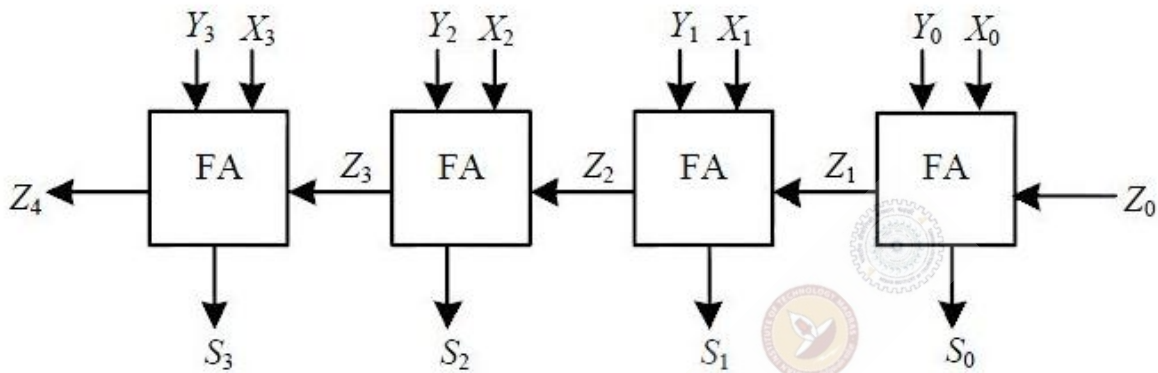


Figure I

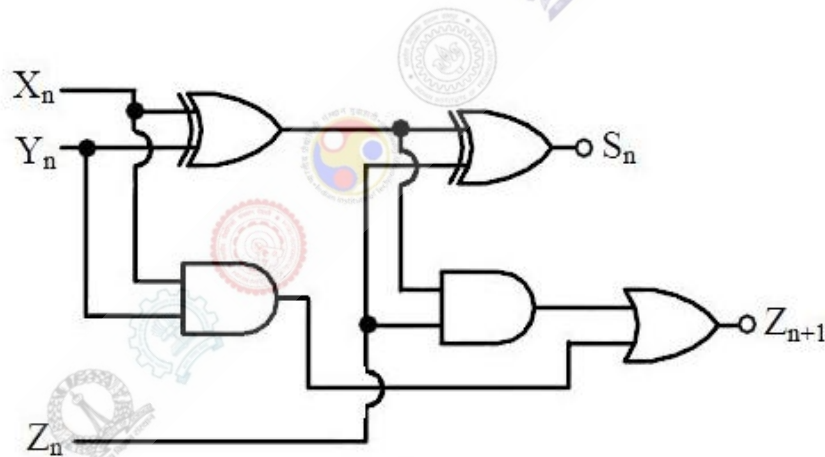
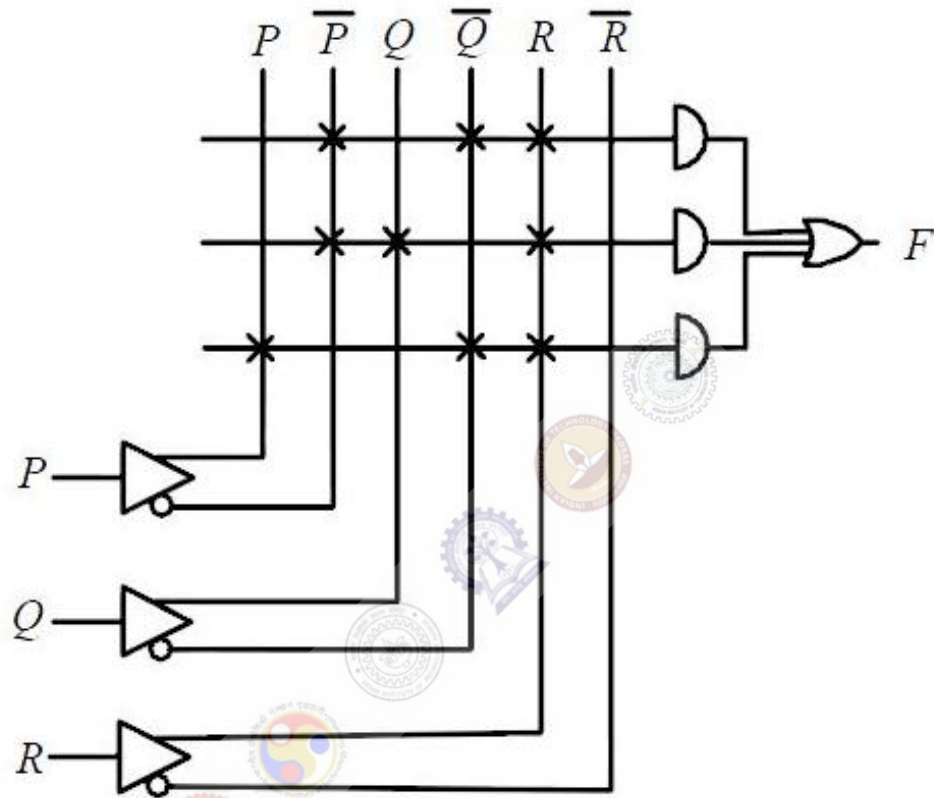


Figure II

At $t = 0$, the inputs to the 4-bit adder are changed to $X_3X_2X_1X_0 = 1100$, $Y_3Y_2Y_1Y_0 = 0100$ and $Z_0 = 1$. The output of the ripple carry adder will be stable at t (in ns) = _____

A programmable logic array (PLA) is shown in the figure.



The Boolean function F implemented is

- (A) $\bar{P} \bar{Q} R + \bar{P} Q R + P \bar{Q} \bar{R}$
- (B) $(\bar{P} + \bar{Q} + R)(\bar{P} + Q + R)(P + \bar{Q} + \bar{R})$
- (C) $\bar{P} \bar{Q} R + \bar{P} Q R + P \bar{Q} R$
- (D) $(\bar{P} + \bar{Q} + R)(\bar{P} + Q + R)(P + \bar{Q} + R)$

Question Number : 46

Correct : 2 Wrong : 0

A unity feedback control system is characterized by the open-loop transfer function

$$G(s) = \frac{2(s + 1)}{s^3 + ks^2 + 2s + 1}$$

The value of k for which the system oscillates at 2 rad/s is _____.

Question Number : 47

Correct : 2 Wrong : -0.66

A second-order LTI system is described by the following state equations,

$$\frac{d}{dt}x_1(t) - x_2(t) = 0$$

$$\frac{d}{dt}x_2(t) + 2x_1(t) + 3x_2(t) = r(t)$$

where $x_1(t)$ and $x_2(t)$ are the two state variables and $r(t)$ denotes the input. The output $c(t) = x_1(t)$. The system is

(A) undamped (oscillatory)

(B) underdamped

(C) critically damped

(D) overdamped

Question Number : 50

Correct : 2 Wrong : 0

The unmodulated carrier power in an AM transmitter is 5 kW. This carrier is modulated by a sinusoidal modulating signal. The maximum percentage of modulation is 50%. If it is reduced to 40%, then the maximum unmodulated carrier power (in kW) that can be used without overloading the transmitter is _____

Question Number : 51

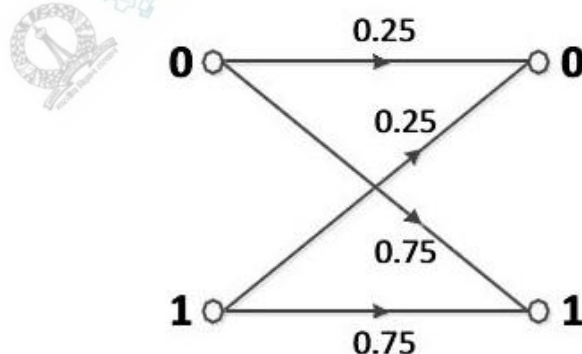
Correct : 2 Wrong : 0

A modulating signal given by $x(t) = 5 \sin(4\pi 10^3 t - 10\pi \cos 2\pi 10^3 t)$ V is fed to a phase modulator with phase deviation constant $k_p = 5$ rad/V. If the carrier frequency is 20 kHz, the instantaneous frequency (in kHz) at $t = 0.5$ ms is _____

Question Number : 52

Correct : 2 Wrong : -0.66

Consider a binary memoryless channel characterized by the transition probability diagram shown in the figure.



The channel is

(A) lossless

(B) noiseless

(C) useless

(D) deterministic

Question Number : 53**Correct : 2 Wrong : 0**

An electron (q_1) is moving in free space with velocity 10^5 m/s towards a stationary electron (q_2) far away. The closest distance that this moving electron gets to the stationary electron before the repulsive force diverts its path is _____ $\times 10^{-8}$ m.

[Given, mass of electron $m = 9.11 \times 10^{-31}$ kg, charge of electron $e = -1.6 \times 10^{-19}$ C, and permittivity $\epsilon_0 = (1/36\pi) \times 10^{-9}$ F/m]

Question Number : 54**Correct : 2 Wrong : -0.66**

Standard air-filled rectangular waveguides of dimensions $a = 2.29$ cm and $b = 1.02$ cm are designed for radar applications. It is desired that these waveguides operate only in the dominant TE_{10} mode with the operating frequency at least 25% above the cutoff frequency of the TE_{10} mode but not higher than 95% of the next higher cutoff frequency. The range of the allowable operating frequency f is

(A) $8.19 \text{ GHz} \leq f \leq 13.1 \text{ GHz}$

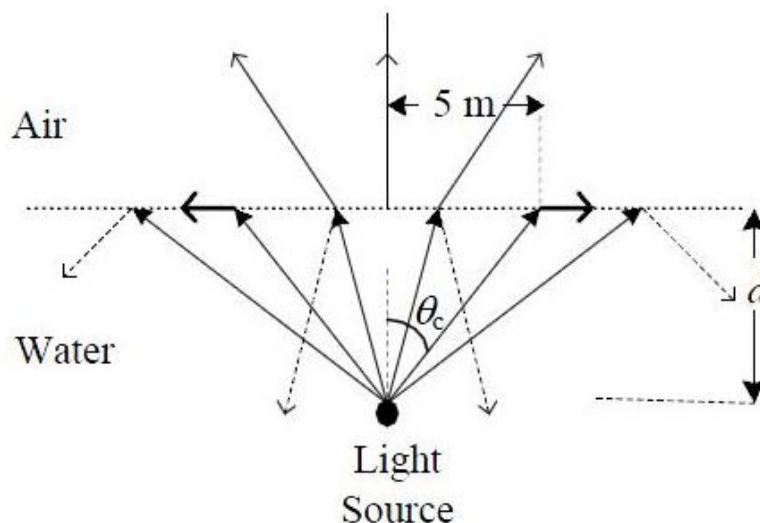
(B) $8.19 \text{ GHz} \leq f \leq 12.45 \text{ GHz}$

(C) $6.55 \text{ GHz} \leq f \leq 13.1 \text{ GHz}$

(D) $1.64 \text{ GHz} \leq f \leq 10.24 \text{ GHz}$

Question Number : 55**Correct : 2 Wrong : 0**

The permittivity of water at optical frequencies is $1.75 \epsilon_0$. It is found that an isotropic light source at a distance d under water forms an illuminated circular area of radius 5 m, as shown in the figure. The critical angle is θ_c .



The value of d (in meter) is _____

Question Number : 56

Correct : 1 Wrong : -0.33

The ninth and the tenth of this month are Monday and Tuesday _____.

- (A) figuratively (B) retrospectively (C) respectively (D) rightfully

Question Number : 57

Correct : 1 Wrong : -0.33

It is _____ to read this year's textbook _____ the last year's.

- (A) easier, than (B) most easy, than (C) easier, from (D) easiest, from

Question Number : 58

Correct : 1 Wrong : -0.33

A rule states that in order to drink beer, one must be over 18 years old. In a bar, there are 4 people. P is 16 years old, Q is 25 years old, R is drinking milkshake and S is drinking a beer. What must be checked to ensure that the rule is being followed?

- (A) Only P's drink
(B) Only P's drink and S's age
(C) Only S's age
(D) Only P's drink, Q's drink and S's age

Question Number : 59

Correct : 1 Wrong : -0.33

Fatima starts from point P, goes North for 3 km, and then East for 4 km to reach point Q. She then turns to face point P and goes 15 km in that direction. She then goes North for 6 km. How far is she from point P, and in which direction should she go to reach point P?

- (A) 8 km, East (B) 12 km, North (C) 6 km, East (D) 10 km, North

Question Number : 64

Correct : 2 Wrong : -0.66

The number of 3-digit numbers such that the digit 1 is never to the immediate right of 2 is

(A) 781

(B) 791

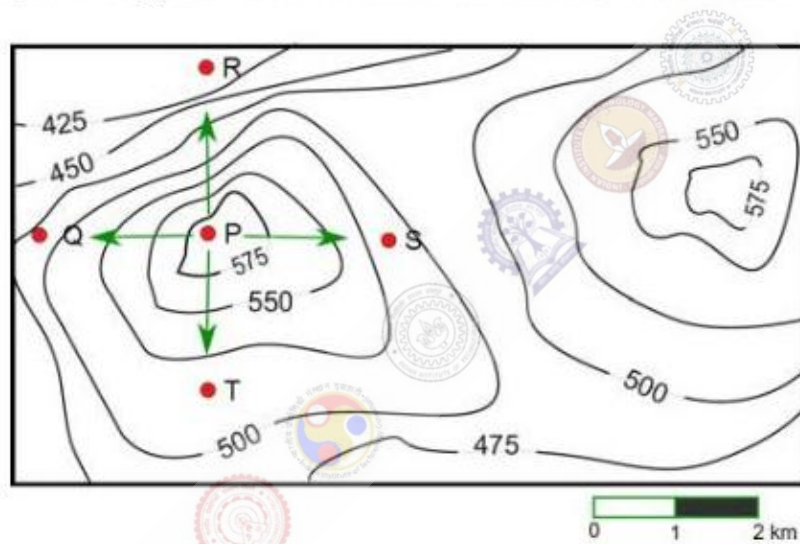
(C) 881

(D) 891

Question Number : 65

Correct : 2 Wrong : -0.66

A contour line joins locations having the same height above the mean sea level. The following is a contour plot of a geographical region. Contour lines are shown at 25 m intervals in this plot.



Which of the following is the steepest path leaving from P?

(A) P to Q

(B) P to R

(C) P to S

(D) P to T